

$$(a+b)^n$$

$$(1+x)^{15}$$

$$\begin{array}{cccccc} & & & 1 & & & \\ & & & | & 2 & | & \\ & & 1 & 3 & 3 & 1 & \\ n=4. & 1 & 4 & 6 & 4 & 1 & \end{array}$$

Find the first 4 terms of  $(1+x)^{15}$ .

Soln:

$$\begin{aligned} (1+x)^{15} &= 1^{15} + 15 \binom{15}{1} x + \frac{15 \times 14}{2} \binom{15}{2} x^2 + \frac{15 \times 14 \times 13}{3!} \binom{15}{3} x^3 + \dots \\ &= 1 + 15x + 105x^2 + 455x^3 + \dots \end{aligned}$$

$$(5-x)^{10} = (5+(-x))^{10}$$

Expand  $a=5$  &  $b=-x$ ,  $n=10$ .

$$\begin{aligned} (5-x)^{10} &= 5^{10} + \binom{10}{1} 5^9 (-x) + \binom{10}{2} 5^8 (-x)^2 + \binom{10}{3} 5^7 (-x)^3 + \dots \\ &= 5^{10} - 10 \cdot 5^9 x + \frac{10 \times 9}{2} 5^8 x^2 - \frac{10 \times 9 \times 8}{3!} 5^7 x^3 + \dots \end{aligned}$$

=

Expand  $\frac{1}{1+x}$

Soln:  $(1+x)^{-1}$ . Substituting  $n=-1$  into

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \frac{n(n-1)(n-2)}{3!}x^3 + \dots$$

$$\begin{aligned}(1+x)^{-1} &= 1 - x + \frac{(-1)(-2)}{2!}x^2 + \frac{(-1)(-2)(-3)}{3!}x^3 \\ &\quad + \frac{(-1)(-2)(-3)(-4)}{4!}x^4 + \dots \\ &= 1 - x + x^2 - x^3 + x^4 - \dots\end{aligned}$$

---

Expand  $(1+x)^{1/2}$ .

Soln:  $(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \frac{n(n-1)(n-2)}{3!}x^3 + \dots$

$$\begin{aligned}(1+x)^{1/2} &= 1 + \frac{1}{2}x + \frac{\frac{1}{2}(\frac{1}{2}-1)}{2!}x^2 + \frac{\frac{1}{2}(\frac{1}{2}-1)(\frac{1}{2}-2)}{3!}x^3 + \dots \\ &= 1 + \frac{1}{2}x + \frac{1}{2}\left(-\frac{1}{2}\right)\frac{1}{2}x^2 + \frac{1}{2}\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\frac{1}{3!}x^3 \\ &= 1 + \frac{1}{2}x + \frac{-x^2}{8} + \frac{x^3}{16} - \dots\end{aligned}$$